QUANTITATIVE ANALYSIS OF OBSERVED SEISMIC STRAINS IN UNDERGROUND STRUCTURES *

by

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SYNOPSIS

The observed seismic strains of several types of underground structures were quantitatively analyzed. A total of 123 seismic records obtained during 91 earthquakes in seven buried pipelines, three submerged tunnels, two embedded tanks and a rock tunnel were The general levels of seismic strains were found to differ according to the types of underground structures. by assuming the seismic strain of buried pipelines to be unity, those of submerged tunnels and embedded tanks were found to be about 0.39 and 0.14, respectively. The seismic strain of buried pipelines was found more strongly correlated with the peak ground velocity than with the ground acceleration. The measured strains were then compared with the calculated strains obtained by the Technical Guidance for Petroleum Pipeline. The calculated strains were found to generally give much higher values than the measured strains, indicating that the present Technical Guidance may be too conservative to estimate the seismic pipe strains.

INTRODUCTION

In recent years, the roles of underground structures, such as buried pipelines, submerged tunnels, embedded tanks and rock tunnels, are becoming increasingly more important in the civil engineering construction. Past studies have shown that the dynamic responses of these structures during earthquakes are greatly influenced by the behavior of the surrounding soil[1-3]. By reflecting the abovementioned finding, the response-displacement method is

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widely used in Japan for the earthquake resistant design of these structures [4-6]. However, the distribution of ground displacement during an earthquake, namely the seismic strain in the ground, has not been well understood today. Therefore, observed data of ground strain during earthquakes supply very important information for the design of underground structures. Although the direct measurement of the seismic ground strain is generally difficult, it has been conclusively shown that the buried pipe strains may in most cases be considered to represent the soil strains during an earthquake[1].

In this paper, the seismic strains produced in underground structures are quantitatively investigated by using the 123 data recorded in Japan. They include the data in seven buried pipelines [7-16], three submerged tunnels[2,17-21], two embedded tanks[3,22,23] and one rock tunnel[24]. In the latter part of the paper, the strains calculated by the method specified in the Technical Guidance for Petroleum Pipeline[4], which is frequently used for the earthquake resistant design of buried pipelines in Japan, are compared with the observed data.

OBSERVED SEISMIC STRAINS IN UNDERGROUND STRUCTURES

OBSERVATION SITES AND EARTHQUAKE RECORDS: The records of the 91 earthquake events from 1970 to 1980 observed at 13 sites for the four types of underground structures were investigated in this study. Table 1 shows the list of the observation sites, types of structures and their relevant properties. The epicenters, depths and magnitudes of the 91 earthquakes are summarized in Table 2. first columns of Tables 1 and 2 assign reference numbers for all the observation sites and earthquakes, respectively. By using these reference numbers, the complete information of the 123 data are summarized in Table 3. There are 60, 48, 9 and 6 observations for buried pipelines, submerged tunnels, embedded tanks and a rock tunnel, respectively. The x and y axes were taken in the horizontal The x axis was taken along the longitudinal direction of a structure for pipes and tunnels and the y axis perpendicular to the The z axis was taken along the vertical direction. 1 in Table 3 indicates the longitudinal axial strain ϵ_{L} for linear structures and the horizontal circumferential strain for embedded STRAIN 2 indicates the circumferential strain for buried pipelines, the bending strain for submerged tunnels and the vertical axial strain for embedded tanks.

CHARACTERISTICS OF OBSERVED SEISMIC STRAINS: Figure 1 shows the cumulative frequency distributions of observed strains ϵ for the four different types of structures. It is clearly seen that the observed strains are the smallest for the rock tunnel and the largest for the buried pipelines.

To examine the effect of acceleration level, the cumulative

frequency distributions of ε/a are plotted in Fig. 2, where a is the measured peak acceleration. When the strains are normalized by the peak accelerations, the curves of buried pipelines and submerged tunnels are found to exhibit almost similar tendencies.

Figure 3 is shown to illustrate the effect of ground conditions on seismic strains. For this purpose, the measured strain was normalized by the product of the peak acceleration a and the natural period of the ground T in the form of $\varepsilon/(\alpha \cdot T/2\pi)$. Since the quantity $\alpha \cdot T/2\pi$ in the denominator has the dimension of velocity, the ratio $\epsilon/(\alpha \cdot T/2\pi)$ may be considered as the strain per unit ground The information contained in Fig. 3 is considered more velocity. general than those in Figs. 1 and 2 because the strain is normalized by the site factor T as well as by the ground shaking intensity α . The seismic strain generally increases in the following order: embedded tanks, rock tunnels, submerged tunnels and buried pipelines. While the rock tunnel gave the smallest strain in Fig. 1, the smallest strain in Fig. 3 corresponds to the embedded tank. This change has probably resulted from the fact that, while the strain in the rock tunnel is almost the same as that in the surrounding rock, the strain in the embedded tank is considerably smaller than that in the surrounding ground[3]. At the 50%-level of the cumulative frequency distribution, the ratios among the strains per unit velocity of pipeline, submerged tunnel and embedded tank are 1:0.39:0.14. though both pipelines and submerged tunnels are linear structures, the strain levels produced during earthquakes are quite different. This is probably due to the difference between their cross-sectional areas.

In Fig. 4, the buried pipelines are divided into two groups according to their diameters, namely $D<1000\,$ mm and $D\geq1000\,$ mm. However, the two curves corresponding to these two groups do not show any significant difference. This seems to indicate that the effect of pipe size is not significant within the diameter range between 160 mm and 1800 mm. Note, however, that this statement cannot be conclusive because of the insufficient number of data available at present.

Measured "axial" strains ε_L of pipes and tunnels are shown in Fig. 5 for the four different groups of earthquake magnitudes (M>7, 7>M>6, 6>M>5 and 5>M) plotted against the epicentral distance. It is interesting to notice that the slope of the regression line for M>7 is smaller than those for 7>M>6 and 6>M>5. This seems to indicate that the strains caused by large earthquakes do not decrease rapidly with the increase in epicentral distance. The regression equations and some relevant quantities are also shown in Fig. 5. Since the effect of ground condition is not considered, the coefficients of correlation are not high.

All the regression equations obtained in this study are summarized in Table 4.

SEISMIC STRAINS IN BURIED PIPELINES

In most cases it is difficult to directly measure the strains in the ground caused by an earthquake. However, past studies have conclusively shown that the strains produced in pipelines during an earthquake are almost the same as those of the surrounding ground[1]. In fact, it is always more practical to estimate the approximate soil strains in the surrounding ground from the measured pipe strains. In this section the observed strains in the buried pipelines during earthquakes are investigated in detail.

The observed "axial" pipe strains ϵ_L are plotted in Fig. 6 against the epicentral distance for the earthquakes with magnitudes equal to or greater than 7. Since the effect of ground condition is not considered, the coefficient of correlation is low (γ =-0.474). Generally, the observed pipe strains in the soft ground with a longer natural period is much higher than those in a harder ground with a shorter natural period. Hence, the pipe strain was normalized by the corresponding natural period of ground. The results are shown in Fig. 7, which shows a considerably higher value of the coefficient of correlation (γ =-0.679).

The axial pipe strains ε_L are plotted against the peak accelerations α_X , α_y and α_Z in Figs. 8, 9 and 10, respectively. The correlations between accelerations and axial strains in these figures are relatively high with the coefficients of correlation γ being 0.756, 0.716 and 0.791 for α_X , α_y and α_Z , respectively. The correlation between ε_L and α_X is again examined in Fig. 11 for the two groups of data classified according to the epicentral distance Δ . The observed data were divided into two groups with $\Delta < 150$ km and $\Delta > 150$ km. It can be easily seen from Fig. 11 that the earthquakes with longer epicentral distances tend to produce higher axial pipe strains for the same acceleration level than those with shorter distances do. This tendency is also apparent in Figs. 9 and 10.

The axial pipe strains are plotted again in Fig. 12 against $a_X \cdot T/2\pi$ in order to approximately take into account the effect of ground condition. The coefficients of correlation γ are found to be much higher than those obtained in Fig. 8, indicating that the axial pipe strains are more strongly correlated to the ground velocity than to the ground acceleration. The coefficient of correlation γ is as high as 0.944 for M>7. As can be seen from Table 3, there are 17 observed strain data for which the ground velocities were also measured. Figure 13 shows the plot of these 17 data against the measured longitudinal peak velocity v_X . The high value of γ =0.898 clearly indicates the strong correlation between the axial pipe strain and the velocity.

DATA FROM THE 1978 MIYAGI-KEN-OKI EARTHQUAKE

During the 1978 Miyagi-ken-oki earthquake (M=7.4), records were

obtained at 8 sites out of the 13 listed in Table 1. At one site, the maximum recorded pipe strain reached 299×10^{-6} .

The measured axial strains of linear structures (buried pipelines and submerged tunnels) are shown in Fig. 14 plotted against the measured peak acceleration a_X . The regression line in Fig. 14 is that obtained from the previous analysis (M>7 in Fig. 8). The regression line obtained by using the peak acceleration as the variable is found to fail to explain the two points at the higher acceleration level.

In Fig. 15, the axial strain ε_L is plotted against the parameter $(\alpha_x \cdot T/2\pi)$ as was done in Fig. 12. The regression line previously obtained in Fig. 12 for M>7 earthquakes now shows a much better agreement with the data especially at the higher strain levels. As can be seen from Tables 1 and 3, the largest observed strain of 299 \times 10⁻⁶ was obtained for α_x =125 gal at the site with T=1.3 sec. The calculated strain for these α_X and T values is 180 \times 10⁻⁶ which is about 60% of the observed value. Although the calculated strain is still small, the agreement in Fig. 15 is considered reasonable.

Figure 16 shows the relations between ϵ_L and T by using the regression line for M>7 obtained in Fig. 12 for several different values of the peak acceleration. By using this figure, for $\alpha_{\rm X}$ =500 gal and T=2 sec, for example, ϵ_L may be easily estimated to be about 1100×10^{-6} . Note, however, that the lines in Fig. 16 are still very tentative because of the lack of observed data.

SEISMIC PIPE STRAINS CALCULATED BY THE TECHNICAL GUIDANCE FOR PETRO-LEUM PIPELINE

In Japan, the earthquake resistant design of buried pipelines is often performed according to the Technical Guidance for Petroleum Pipeline[4,25,26]. A buried pipeline in the x direction as shown in Fig. 17 is considered. A shear wave with a wave length L and a displacement amplitude U is assumed to propagate in the direction of the x' axis, which makes an angle of ϕ with the pipe axis. The amplitude U is decomposed into two components U_L and U_B , where U_L is the component in the pipe direction (x-axis) and U_B is the component perpendicular to the pipe direction.

$$U_{L} = U \cdot \sin\phi \cdot \sin\left[\frac{2\pi \cdot \cos\phi}{L}x\right] \tag{1}$$

$$U_{R} = U \cdot \cos\phi \cdot \sin\left[\frac{2\pi \cdot \cos\phi}{L}x\right] \tag{2}$$

The longitudinal axial strain e_L and the transverse bending strain e_B of the virtual soil pipeline are obtained by

$$e_L = \frac{\partial U_L}{\partial x} = \frac{2\pi \cdot U}{L} \sin\phi \cdot \cos\phi \cdot \cos\left[\frac{2\pi \cdot \cos\phi}{L} x\right]$$
 (3)

$$e_B = \frac{D/2}{\rho} = \frac{2\pi^2 \cdot D \cdot U}{L^2} \cos^3 \phi \cdot \sin\left[\frac{2\pi \cdot \cos \phi}{L}x\right] \tag{4}$$

where ${\it D}$ is the pipe diameter, and the radius of curvature ρ of pipe is obtained from

$$\frac{1}{\rho} = \frac{\partial^2 U_B}{\partial x^2} \tag{5}$$

By putting $\cos\left[\frac{2\pi\cdot\cos\phi}{L}x\right]$ and $\sin\left[\frac{2\pi\cdot\cos\phi}{L}x\right]$ equal to unity in Eqs. (3) and (4), respectively, it is found

$$e_L = \frac{2\pi \cdot U}{L} \sin\phi \cdot \cos\phi \tag{6}$$

$$e_B = \frac{2\pi^2 \cdot D \cdot U}{L^2} \cos^3 \phi \tag{7}$$

The maximum values of e_L and e_B denoted by e_{Lmax} and e_{Bmax} , respectively, become

$$e_{Lmax} = \frac{\pi \cdot U}{L} \qquad (\phi = \frac{\pi}{4}) \tag{8}$$

$$e_{Bmax} = \frac{2\pi^2 \cdot D \cdot U}{L^2} \qquad (\phi = 0) \tag{9}$$

The factors of transmission to convert these ground strains to the pipeline strains are determined by considering the physical properties of the pipeline, the surrounding soil and the propagating wave. The factors α_1 and α_2 for the longitudinal axial and the transverse bending strain, respectively, are

$$\alpha_1 = \frac{1}{1 + \frac{2\pi^2}{L^2} \cdot \frac{E \cdot S}{K_1}} \tag{10}$$

$$\alpha_2 = \frac{1}{1 + \frac{16\pi^{\frac{1}{4}} \cdot E \cdot I}{L^{\frac{1}{4}}} \cdot \frac{E \cdot I}{K_2}}$$
 (11)

where

E = Young's modulus of pipe

S = Cross-sectional area of pipe

I = Moment of inertia of pipe

- K_1 = Force per unit surface area of pipe that produces a unit of relative axial displacement between pipe and soil
- K_2 = Force per unit surface area of pipe that produces a unit of relative lateral displacement between pipe and soil

Generally speaking, the values of α_1 and α_2 are almost equal to 1 for most practical cases. Therefore, the strains produced in a buried pipeline may be assumed to be approximately equal to the strains of the ground.

According to the Technical Guidance, the design strain e_T is obtained by

$$e_{T} = \sqrt{2(1^{2} + 0.75^{2})(\alpha_{1} \cdot e_{Lmax})^{2} + (\alpha_{2} \cdot e_{Bmax})^{2}}$$

$$= \sqrt{3.12(\alpha_{1} \cdot e_{Lmax})^{2} + (\alpha_{2} \cdot e_{Bmax})^{2}}$$
(12)

where the pipe is assumed to be simultaneously subjected to five incident shear waves.

The displacement amplitude ${\it U}$ appearing in the previous equations is calculated by

$$U = \frac{2}{\pi^2} \cdot T \cdot S_V \cdot K_{Oh} \tag{13}$$

where

T = Natural period of ground

 K_{oh} = Seismic coefficient to be assumed at the base ground

 S_V = Velocity response spectral amplitude of the ground motion with a peak acceleration of 1 g (g = acceleration of gravity)

The natural period of ground T is calculated by

$$T = 4 \Sigma \frac{H_i}{V_{Si}} \tag{14}$$

where

 H_i = Thickness of the *i*-th layer

 V_{si} = Shear wave velocity of the *i*-th layer

The velocity response spectum $(S_{\mathbf{V}})$ to be used in Eq.(13) is shown in Fig. 18.

According to the flow chart shown in Fig. 19, the strains calculated by the Technical Guidance were compared with the observed buried pipe strains ε_L . Since the strains are first calculated by assuming an input acceleration of $A=U(2\pi/T)^2$, the values e_{Lmax} and e_T must be multiplied by a factor $C=\alpha_X/A$ before they are compared with the observed strains. The symbols e_{CG} , e_{CL} and e_{CT} used in the following part are $C \cdot e_{Lmax}$, $C \cdot \alpha_1 \cdot e_{Lmax}$ and $C \cdot e_T$, respectively.

The cumulative frequency distributions of e_{CG}/ε_L , e_{CL}/ε_L and e_{CT}/ε_L are shown in Fig. 20. For the 50%-level on the vertical scale the values of e_{CL}/ε_L , e_{CG}/ε_L and e_{CT}/ε_L are 2.5, 2.7 and 4.3, respectively. It is interesting to note that e_T obtained from the Technical Guidance is 4.3 times larger than observed value.

Figure 20 also shows the cumulative frequency distribution curve e_P/ε_L , in which the calculated strain e_P was obtained by the method proposed by the authors[27,28,29]. The value of e_P/ε_L at the 50%-level is approximately 1.5, indicating that the calculated strain e_P is much closer to the observed value than the strains by the Technical Guidance are.

The greatest pipe strain (299×10^{-6}) during the Miyagi-ken-oki earthquake was observed at the Shimonaga site as shown in Table 1. The strains calculated by the method of the Technical Guidance $(e_{CL}, e_{CG} \text{ and } e_{CT})$ and the authors' method (e_P) as well as observed data during several earthquakes are shown in Fig. 21. The Shimonaga site is covered with a 40 m soft surface layer with an average N-value of 7[11]. This surface layer is composed of peat, soft sandy and silty soils.

All the calculated strains are larger than the observed ones. Moreover, the values e_{CT} calculated by the method of the Technical Guidance show the greatest difference, while the values e_P calculated by the authors' method show the smallest difference. The observed data (earthquake magnitudes, pipe strains and peak accelerations) and the ratios e_P/ε_L , e_{CL}/ε_L , e_{CC}/ε_L and e_{CT}/ε_L are shown in Table 5. It seems interesting to note that as the magnitudes of earthquakes increase the ratios between the calculated and the measured strain decrease. For example, the ratios e_{CT}/ε_L for M=5.8 and 7.4 are 22.8 and 3, respectively. In any case, it is important to accumulate more observed data, especially those produced by large magnitude earthquakes in order to make a more reliable estimate of the seismic strains of buried pipelines.

CONCLUSIONS

In this paper, seismic strains observed in several kinds of underground structures (buried pipelines, submerged tunnels, embedded tanks and a rock tunnel) were investigated, and the strains calculated by the Technical Guidance for Petroleum Pipeline in Japan

were compared with the observed strains. Major points of interest found from the study reported in this paper are summarized below.

- (1) The level of the normalized seismic strains $\varepsilon/(a \cdot T/2\pi)$ generally differ according to the different types of underground structures. Supposing that the strain in a buried pipeline is 1, the strains in a submerged tunnel and an embedded tank are 0.39 and 0.14, respectively.
- (2) The decrease of the seismic strain of buried structures with distance is slower for large magnitude earthquakes than for smaller earthquakes.
- (3) For the same level of the peak acceleration (or velocity), the seismic strain increases with the earthquake magnitude and the epicentral distance.
- (4) The axial strain ε_L in a buried pipeline is more strongly correlated with the peak ground velocity v_X or $(\alpha_X \cdot T/2\pi)$ than with the peak ground acceleration α_X . The regression line obtained for M>7 earthquakes was

$$\log \varepsilon_L = 1.02 \cdot \log \frac{\alpha_X \cdot T}{2\pi} + 0.804$$

with a surprisingly high value of the coefficient of correlation of 0.94.

(5) The compound axial strain e_{CT} calculated by the Technical Guidance for Petroleum Pipeline is, on average, 4 times greater than the observed strain.

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NOTATION

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\boldsymbol{A}
      ; Acceleration amplitude used in the Technical Guidance for
        Petroleum Pipeline (cm/sec<sup>2</sup>)
      ; Measured peak ground acceleration (cm/sec<sup>2</sup>)
\alpha_{x}, \alpha_{y}, \alpha_{z}; Measured peak acceleration of a pipeline in the x, y and
            z direction, respectively (cm/sec<sup>2</sup>)
C
      ; \alpha_{\mathbf{x}}/A
D
      ; Pipe diameter (cm)
      ; Young's modulus of pipe (kg/cm<sup>2</sup>)
      ; Calculated strain
      ; Ground strain corresponding to K_{Oh}=1 that causes bending strain
e_B
        in pipe
e_{Bmax}; Maximum of e_B (\phi=0)
e_{CG} ; Axial strain \mathcal{C} \cdot e_{I,max} of ground calculated by the Technical
        Guidance
      ; Axial strain C \cdot \alpha_1 \cdot e_{I,max} of pipe calculated by the Technical
e_{CL}
        Guidance
      ; Compound strain C \cdot e_T of pipe calculated by the Technical
        Guidance
      ; Ground strain in axial direction of pipeline
e_L
e_{Lmax}; Maximum of e_L (\phi=\pi/4)
      ; Ground strain calculated by the authors' method
      ; Compound strain of pipe calculated by the Technical Guidance
e_T
H_{m{i}}
      ; Thickness of the i-th layer (cm)
      : Moment of inertia of pipe (cm<sup>4</sup>)
      ; Force per unit surface area of pipe that produces a unit of
        relative axial displacement between pipe and soil (kg/cm<sup>2</sup>)
      ; Force per unit surface area of pipe that produces a unit of
K_2
        relative lateral displacement between pipe and soil (kg/cm<sup>2</sup>)
      ; Seismic coefficient at the design foundation
K_{Oh}
L
      ; Wave length (cm)
      ; Earthquake magnitude
Μ
      ; Number of data
17
      ; Cross-sectional area of pipe (cm<sup>2</sup>)
S
      ; Response velocity at the ground surface for K_{Oh}=1 (cm/sec)
S_{f v}
      ; Natural period of ground (sec)
      ; Horizontal displacement amplitude at ground surface (cm)
U
      ; Displacement amplitude of ground in y-direction (cm)
U_B
      : Displacement amplitude of ground in x-direction (cm)
U_{L}
      ; Shear wave velocity of the i-th layer (cm/sec)
v_x, v_y; Peak velocities of pipeline in x and y direction, respectively
        (cm/sec)
      ; Axis along buried pipeline
x'
      ; Direction of wave propagation
      ; Axis perpendicular to x axis
y
      : Vertical axis
      ; Factor of transmission of axial strain from soil to pipe
      ; Factor of transmission of bending strain from soil to pipe
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 γ ; Coefficient of correlation Δ ; Epicentral distance (km)

ε ; Measured strain

 ε_L ; Measured axial strain

ρ ; Radius of curvature of pipe (cm)

σ ; Standard deviation about regression line

 ϕ ; Angle between the pipeline axis and the direction of earth-

quake wave propagation (radian)

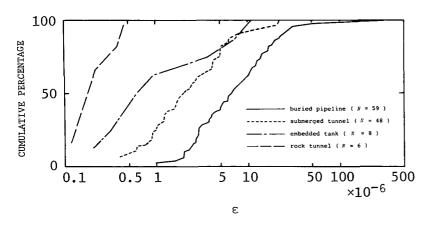


Fig.1. Cumulative Frequency Distribution Curves for $\boldsymbol{\epsilon}$

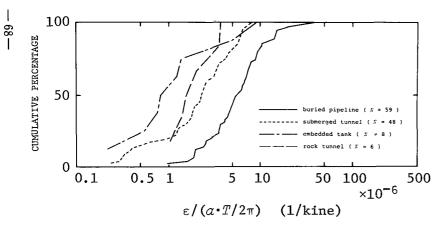


Fig.3. Cumulative Frequency Distribution Curves for $\varepsilon/(\alpha \cdot T/2\pi)$

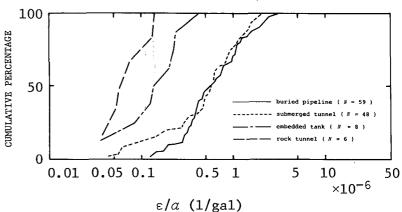


Fig.2. Cumulative Frequency Distribution Curves for ϵ/α

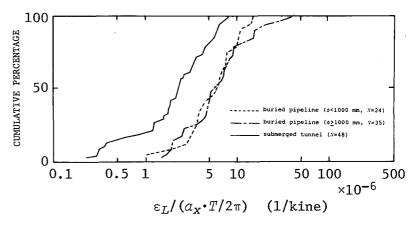


Fig.4. Cumulative Frequency Distribution Curves for $\varepsilon_L/(\alpha_x \cdot T/2\pi)$ (Submerged Tunnels and Buried Pipelines with D<1000 and D>1000)

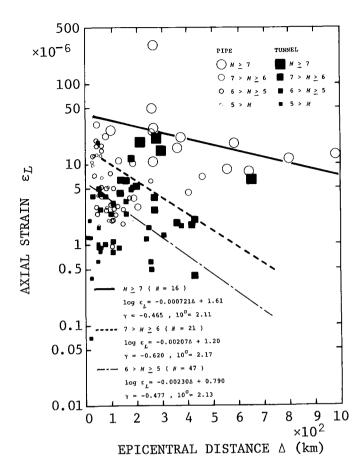


Fig. 5. Relation between Axial Strain and Epicentral Distance for Linear Underground Structures

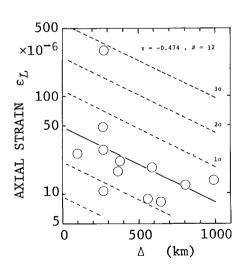


Fig.6. Relation between Axial Pipe Strain and Epicentral Distance (M>7)

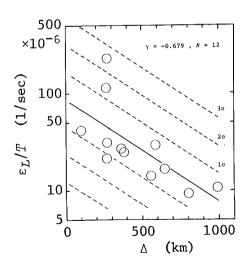


Fig. 7. Relation between ε_L/T and Epicentral Distance for Pipelines $(M \ge 7)$

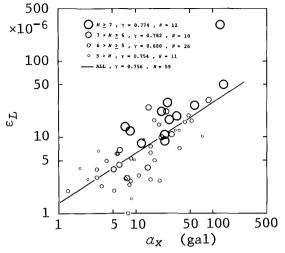
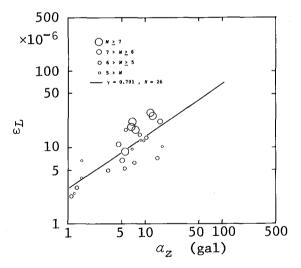
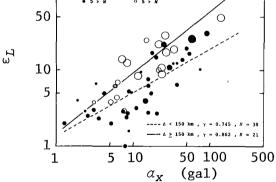


Fig. 8. Relation between Axial Pipe Strain and Longitudinal Peak Acceleration

Fig.9. Relation between Axial
Pipe Strain and Lateral
Peak Acceleration

0





500 ×10⁻⁶

100

Fig.10. Relation between Axial Pipe Strain and Vertical Peak Acceleration

Fig.11. Relation between Axial
Pipe Strain and
Longitudinal Peak
Acceleration
(Δ<150 km and Δ>150 km)

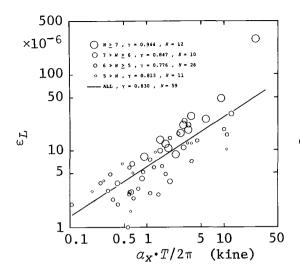
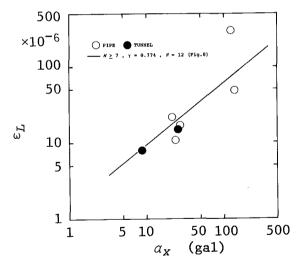


Fig.12. Relation between Axial Pipe Strain and $\alpha_{\rm X} {\circ} T/2\pi$

Fig.13. Relation between Axial Pipe Strain and Peak Velocity $v_{\rm X}$



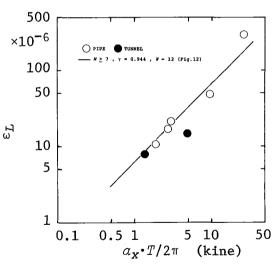


Fig.14. Observed Axial Strain in Linear Structures and Longitudinal Peak Acceleration $\alpha_{\rm X}$ during the Miyagi-ken-oki Earthquake

Fig.15. Observed Axial Strain in Linear Structures versus $\alpha_{\rm X}{\cdot}T/2\pi$ for the Data Obtained from the Miyagi -ken-oki Earthquake

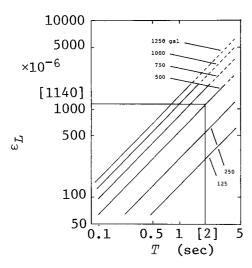


Fig.16. Relation between ε_L and T for Various Levels of α_X Obtained by the Regression Equation (M>7) in Fig.12.

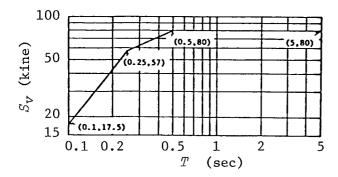


Fig.18. Design Velocity Response Spectrum for Motion with Peak Acceleration 1 g (Technical Guidance for Petroleum Pipeline)

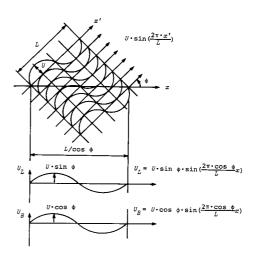


Fig.17. Concept of Pipeline Design for Propagating Seismic Waves

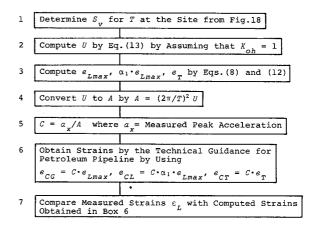


Fig.19. Flow Chart of Comparison between Observed and Calculated Strains

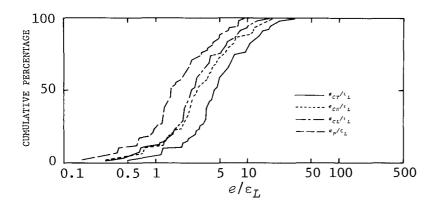


Fig.20. Cumulative Frequency Distributions of e/ϵ_L (= Calculated/Measured)

Table 1. Observation Sites and Types of Underground Structures

מא.	SITE	STRUCTURE	T (SEC)	DIAMETER (MM)	THICKNESS (MM)
1 2	YOKOHAMA SOOKA	PIPE PIPE	0.914	165.2 406.4	5.0
3	OOMORI	PIPE	0.632	216.3	7.9 5.8
4	KANSEN	PIPE	0.437	1554.0	18.0
5	SHIMONAGA	PIPE	1.310	1041.0	13.0
6	HACHINOHE	PIPE	0.504	1219.2	16.0
7	MINAMIWATARIDA	PIPE	0.878	1838.0	19.0
8	HANEDA	TUNNEL	1.600		
9	KINUURA	TUNNEL	0.969		
10	OOGISHIMA	TUNNEL	1.220		
11	NEGISHI	TANK	0.294		
12	SHIMIZU	TANK	1.020		
13	ISHIZUKAYAMA	ROCK TUNNEL	0.229		

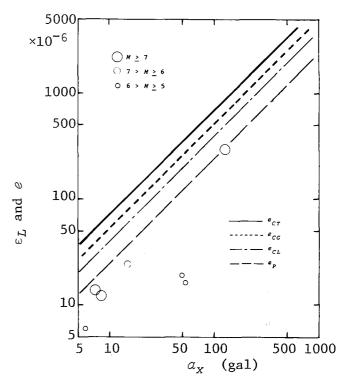


Fig. 21. Various Calculated Strains and Observed Strains for the Data Recorded at the Shimonaga Site

Table 2. List of Earthquakes

NO.	DATE		EPICENTER N E		DEPTH (KM)	MAGNITUDE	
1	1970	9	14	38.68	142.33	40.	6.2
2	1970	9	30	35.48	139.63	40.	4.8
3	1972	1	4	35.87	140.53	40.	5.0
انا	1972	1	27	35.68	139.12	40.	4.8
5	1972	8	31	35.88	136.27	10.	6-0
6	1972	9	25	38.35	142.07	50.	5.5
5	1972	10	6	34.40	138.52	30.	5.5
8	1972	11	5	_	_	50.	3.5
9	1972	11	6	36.20	139.80	40.	5.1
10	1972	12	4	33.20	141.08	50.	7.3
l ii '	1972	12	8	35.58	140.00	90.	4.8
112	1973	1	17			ó0.	4.1
113	1973	- 1	21	36.05	139.87	70.	4.8
14	1973	2	10	33.35	140.72	30.	5.1
15	1973	3	17	36.95	141-68	50.	5.3
16	1973	3	27	35.52	139.93	60.	4.9
17	1973	4	25	33.53	140-87	50.	5.5
18	1973	8	24	36.52	139.75	110.	5.0
19	1973	9	30	35.65	140.67	50.	5.9
20	1973	10	1	35.62	140.80	60.	5.8
21	1973	11	19	38.88	142.15	50.	6.4
22	1973	11	25	33.85	135.42	60.	5.9
23	1973	1.1	25	33.88	135.38	60.	5.8
24	1973	12	22	35.22	140.28	70.	5.0
25	1974	2	10	35.03	136.93	40.	5.3
26	1974	2	22	33.13	137.12	400.	6.9
27	1974	3	. 3	35.08	140,15	40.	6.0
28	1974	5	5	37.75	141.85	40.	5.5
29	1974	5	9	34.57	138.80	10.	6.9
30	1974	6	27	33.75	139.20	10.	6.1
31	1974	7	8	36.42	141,20	40.	6.3
32	1974	8	4	36.02	139,92	50.	5.8
33	1974	8	16	35.25	136.18	50.	4.9
34	1974	9	27	33.72	141.55	60.	6.4
35	1974	10	9	36.05	139.92	60.	4.8
36	1974	10	29	35.60	140.33	70.	4.9
37	1974	10	31	36.10	139.95	60.	4.6
38	1974	11	1	35.60	140.33	60.	4.3
39	1974	11	16	35.60	140.33	40.	6.1
40	974	11	21	35.62	140.33	60.	4.7
41	1974	11	30	30.60	138.27	420.	7.6
1 42	1975	1	14	35.25	141.22	30.	5.1
43	1975	,	21	34.78	141.35	30.	5.9
44	1975	2	- 8	35.82	140.12	460.	5.4
45	1975	3	11	36.52	139.72	130.	5.1
45	1975	3	14	35.30	136.83	50.	5.3

ю.	DATE		DATE EPICENTER N E		DEPTH (KM)	MAGNITUDE	
47	1975	4	12	36.17	140.02	50.	4.0
48	1975	4	18	36.13	139.85	50.	5.0
49	1975	6	16	40.13	142.25	30.	4.9
50	1975	6	18	40.16	142.43	40.	5.0
51	1975	6	18	40.87	143.25	30.	5.5
52	1975	8	12	31.70	138.30	360.	6.9
53	1975	9	20	_		50.	5.9
54	1975	10	30	41.95	142.78	60.	6.0
55	1975	12	15	35.50	140.20	60.	4.6
56	1976	3	15	40.97	141.97	60.	4.3
57	1976	5	13	35.70	139.80	40.	4.2
58	1976	6	2	41.45	142.03	60.	5.0
59	1976	6	16	35.52	139.00	20.	4.7
60	1976	6	16	35.50	139.00	20.	5.5
61	1976	7	8	40.23	142.43	30.	5.9
62	1976	8	18	34.77	138.93	0.	5.5
63	1976	12	29	36.80	139.20	140.	5.8
64	1977	2	4	35.08	138.28	10.	4.2
65	1977	2	18	41.45	141.97	60.	5.4
66	1977	4	25	40.08	142.68	30.	5.0
67	1977	6	4	35.52	140.05	60.	4.6
8	1977	9	28		_	60.	4.8
69	1977	10	5	36.13	139.87	60.	5.4
70	1977	12	17	36.58	141.08	50.	5.6
71	1978	- 1	14	34.77	139.25	10.	7.0
72	1978	1	15	34.83	138.88	20.	5.8
73	1978	1	15	34.80	138.83	10.	5.4
74	1978	2	20	38.20	142.70	50.	6.7
75	1978	3	7	31.60	137.80	440.	7.8
76	1978	3	20	36.10	139.90	60.	5.5
77	1978	3	25	44.33	149.82	40.	7.3
78	1978	4	7	35.20	141.10	40.	5.7
79	1978	5	15	40.20	142.50	40.	5.0
80	1978	5	16	40.95	141.47	10.	5.8
81	197B	5	16	40.93	141.45	10.	5.8
82	1978	6	12	38.15	142,22	30.	7.4
83	1978	6	12	38.20	142.30	40.	5.8
84	1978	6	12	_	_		I —
85	1978	6	14	38.35	142.48	40.	6.3
86	1978	6	21	38.25	142.00	50.	5.8
87	1978	12	6	l —	_	100.	7.7
88	1980	6	29	34.92	139.23	10.	6.7
89	1980	9	24	36.10	139.70	60.	6.0
90	1980	9	25	35.50	140.20	70.	6.1
91	1978	4	7	35.00	141.05	40.	l —

Table 3. Summary of Observed Data

DATA NO.	3118 . ON	EARTHOUAKE NO.	MAGNI TUDE	EFICENTRAL DISTANCE	ACCELERATION (GAL)				OCITY	STRAIN *	
""		110.		(KM)	x	Y	Z	x K	INE) Y	STRAINT	STRAIN2
1 2	1	8 9	3.5 5.1	50. 65.	1.9	2.3	1.5	112414		4.00	******
3	1	10	7.3	270.	26.0	26.0		*****		28.40	******
4	1	12	4.1	60.	*****			4 * 1 * 4 *		12.30	*****
5 6	1	13· 16	4.8 4.9	65.	3.3	8.8		*1 *1 *4		6.70	******
7	2	37	4.6	26. 35.	73.7 32.9	38.8 41.5		3 2 2 2 3 2	* 1 * 1 * 4 *	10.30	0.70
8	2	39	6.1	130.	29.5	29.0				11.00	3.80
9	2	41	7.6	588.	33.8	19.0		*1*19*		18.70	4.20
10	2 2	44 47	5.4 4.0	28.	43.8	16.4			*111##	13.60	3.90
12	2	48	5.0	44. 36.	36.7 37.0	39.0 49.5		*****		12.50 7.30	4.50 2.80
13	2	52	6.9	460.	6.3	9.7		311114		6.80	2.30
14	3	63	5.8	146.	15.5	15.9		381834		6.30	11++1+
15	3	67	4.6	29.	12.6	18.9	6.7		144***	9.50	******
12	3	69 20	5.4 5.6	66. 167.	19.8 5.9	20.5 6.8		*****		14.20	******
18	3	71	7.0	100.	57.9	35.3		44444		26.10	111111
19	3	72	5.8	114.	17.3	8.4	3.3	*14474		5.00	****
20	3	23	5.4	120.	3.6	2.9		****		2.30	*****
21	3	75 76	7.8 5.5	559. 63.	23.4 8.8	18.1 8.2		******		8.90 5.30	******
23	3	78	5.7	129.	3.1	3.0		*****		3.00	*****
24	3	91	****	140.	2.6	2.5		ı.		2.50	******
25	3	82	7.4	365.	27.0	21.7		*****		17.00	******
26	4	49 50	4.9 5.0	89. 99.	9.5		755557 75557	0.53	0.73	5.10 2.20	*******
28	4	51	5.5	148.	15.6 8.5		141114	0.70	1.10	2.70	1711714
29	4	54	6.0	184.	21.4	24.4	*****	1.66	1.61	10.00	******
30	4	56	4.3	56.	8.8		*****	0.26	0.27	1.60	*****
31	4	58 61	5.0 5.9	105.	8.0		*****	0.44	0.62	0.96 2.70	******
33	4	65	5.4	85. 114.	20.3 15.7		*****	1.41	1.20	2.80	2414342
34	4	66	5.0	108.	11.1		*****	0.64	0.53	3.20	*****
35	4	82	7.4	265.	137.5		*****	9.70	7.70	48.90	*****
36	5 5	75 77	7.8 7.3	992. 805.	7.2 8.3		*****	1.18	0.78	13.90 12.20	1111111
38	5	80	5.8	45.	52.8		171788	3.22	1.06	16.50	******
39	5	81	5.8	44.	48.6		*****	2.84	2.80	19.40	*****
40	5	82	7.4	272.	125.1		*****	15.00	12.00	299.20	144444
41	5 5	85 86	6.3 5.8	258.	14.8 5.9		******	2.33	3.24	24.80	******
43	6	49	4.9	258. 87.		*****		*****	0.71	6.10 2.90	******
44	6	51	5.5	150.		*****		*****		1.80	1878787
45	6	53	5.9	176.		*****		*****		3.80	*****
46	6	54	6.0	190.		*****		****		3.80	******
47	6	58 61	5.0 5.9	111. 84.		*****		******		2.00 5.00	444444
49	6	65	5.4	109.				****		2.00	******
50	6	68	4.8	91.				* * * * * *		2.00	*****
51 52	6	74 90	6.7	205.		*****		34149# 34149#		2,90	******
53	6	80 81	5.8 5.8	48. 46.		1 * * * * * * * * * * * * * * * * * * *		*****		2.40 2.90	1111111
54	6	82	7.4	269.				111111		10.70	******
55	6	87	7.7	646.				343294		8.40	*****
56	7	74	6.7	406.	6.2			*111*4		4.35	111111
57 58	7	82 88	7.4 6.7	379. <i>1</i> 8.	21.4 25.0	28.0 26.7		111111 11111		21.80 22.00	111111
59	7	87	6.0	67.	14.4	19.5	111111	\$12786	*****	4.00	111111
60	7	90	6.1	44.	90.0	71.0	\$ 1 \$ 1 \$ ¹	313611	111111	31.00	1153418

	PIPE	TUNNEL	TANK	ROCK TUNNEL
STRAIN1	LONGITUDINAL AXIAL STRAIN	LONGITUDINAL AXIAL STRAIN	HORIZONTAL CIRCUMFERENTIAL STRAIN	LONGITUDINAL AXIAL STRAIN
STRAIN2	CIRCUMFERENTIAL STRAIN	BENDING STRAIN	VERTICAL AXIAL STRAIN	

Table 3. Summary of Observed Data (Continued)

DATA	SITE	EARTHQUAKE	MAGNI TUDE	EFICENTRAL	ACCELERATION	VELOCITY	SIRAIN
ΝΟ.	NO.	иО.		DISTANCE	(GAL)	(KINE)	(MICRO)
	'			(KH)	X Y Z	X Y	STRAINS STRAINS
61	8	1	6.2	420.	2.6 ##1#1# ###1#	4 211114 21414	1.70 *****
62	8	2	4.8	12.	12,1 ****** ****		1.20 *****
63	8	3	5.0	80.	. 4.8 ***** 15141		1.00 ******
64	8	4	4.8	60.	6.8 ***** ****		0.80 *****
65	8	5	6.0	270.	2.3 811414 (4144		2.60 *144**
66	8	6	5.5	380.	1.6 ***** ****		1.20 ******
67	8	7	5.5	160.	10.9 ****** ****		3.50 1*****
68	8	10	7.3	280.	14.7 343444 14344		20.90 44****
69 70	B B	11	4.8 4.8	20. 55.	2.7 ***** 4***		1.60 1144
71	8	14	5.1	260.	0.9 343444 14444		0.50 ******
72	8	15	5.3	240.	0.6 417418 92741		1.20 444444
73	8	16	4.9	17.	13.6 ***** ****	* *****	2.00 *****
74	8	17	5.5	250.	1.2 ****** ****	* ****** ****	1.60 *****
75	8	18	5.0	110.	1.9 47**** 7***		1.10 ******
76	8	19	5.9	80.	4.5 ****** ****		4,00 11****
77	8	20	5.8	100.	4.5 ***** ****		2.40 *****
78	8	21	6.4	430.	1.8 3111441 41444		2.00 ++***
79	8	24	5.0	60.	6.9 \$4**** ***** 3.8 ***** ****		4.20 ******
80 81	8	26 27	6.9	360. 135.	5.1 344444 1144		4.20 17174
81	8	27	5.5	310.	0.9 ***** ****		1.30 *****
83	8	29	6.9	180.	9.3 444444 44444		11.60 ******
84	8	30	6.1	200.	2.9 ****** ****		5.20 *****
85	8	31	6.3	160.	3.8 ****** ****		6.10 *****
86	l š	32	5.8	55.	11.0 ***** ***	* *****	5,00 *****
87	8	34	6.4	270.	7.8 ***** ****		4.80 *****
88	8	35	4.8	60.	2.0 ****** ****		0.90 3#####
89	8	36	4.9	50.	2.4 ***** ****		1.00 *****
90	8	38	4.3	50.	2.1 34**** ****		0.60 ****** A.10 ******
91	8	39	6.1	140.	9.0 ****** ***** 2.0 ****** ****		6.10 ******
92	8	40 42	4.7 5.1	50. 135.	1.0 ****** ****		0.70 111111
93 94	8	43	5.9	160.	2.8 ****** ***		2.40 *****
95	B	1 44	5.4	60.	8.8 ****** ****		2.70 111111
96	l š	45	5.1	110.	2.0 ****** ****		0.80 #11**
97	l š	46	5.3	260.	0.4 319111 3171		0.60 *****
98	9	22	5.9	185.		B ***** *****	5.00 11***
99	9	23	5.8	185.		1 44444 44444	5.00 *****
100	9	25	5.3	30.		8 334434 343444	4.00 *****
101	9	33	4.9	50.		8 ****** *****	6.80 ****** 21.50 ******
102	9	71	7.0	215.		6 *15*** 1225**	21.50 ****** 8.00 *****
103	9	82 52	7.4 6.9	655. 430.	8.7 ****** 4.	7 449484 484144	0.40 0.2
104	10	52	4.6	25.	6.4 334334 3434		0.38 0.5
105	10	57	4.0	22.	1.6 414414 4444		0.07 #####
107	10	60	5.5	110.	19.2 4***** ****		3.20 1.6
108	1 10	82	7.4	300.	24.9 ****** ****		15.00 5.0
109	11	21	7.0	70.	45.5 #3#### 22	.2 ****** *****	10.60 4.6
110	11	82	7.4	370.		8 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	7.00 3.3
111	1.2	39	6.1	260.	3.0 111111 1111		0.60 111111
112	12	41	7.6	540.	1.9 ***** ****		0.44 111111
113	12	59	4.7	70.	1.7 ****** **** 3.7 ***** ****		0.21 ******
114	12	60	5.5	70. 50.	3.7 311434 1344 313143 112344 1244		0.62 411444
115	12	62	5.5 4.2	35.	9.0 +249.44 +449		0.32 141144
117	12	71	7.0	80.	41.9 :14:444 4141		3.59 111141
118	13	79	5.0	120.	1.1 444414 4444		0.15 144444
119	13	80	5.8	190.	1.4 \$19159 \$511		0.18 *****
120	13	83	5.8	120.	3,8 (4)144 1141		0.22 *****
121	13	84	4 2 4 3	11111		18 118141 113814	0.12 111111
122	13	85	6.3	110.	5,2 (1) (1) (1)		0.39 +++++
123	13	86	5.8	105.	8,9 11111 4111		0.46 *****

Table 4. Summary of Regression Lines ($Y=\beta X+\alpha$)

Fig.	Condition	N	Υ	Y	Х	В	α	σ _Y	10 ⁰ Y
5	M≥7	16	-0.465	$\log \epsilon_L$	Δ	-0.000721	1.61	0.325	2.11
5	7 <i>>M</i> <u>></u> 6	21	-0.620	$\log \epsilon_L$	Δ	-0.00207	1.20	0.336	2.17
5	6>M>5	47	-0.477	$\log \epsilon_L^{L}$	Δ	-0.00230	0.790	0.328	2.13
6		12	-0.474	$\log \epsilon_L^{L}$	Δ	-0.000767	1.69	0.357	2.28
7	_	12	-0.679	$\log (\epsilon_L/T)$	Δ	-0.00105	1.94	0.283	1.92
8	_	59	0.756	$\log \epsilon_L$	log a	0.661	0.139	0.287	1.94
8	M≥7	12	0.774	$\log \epsilon_L$	log a	0.808	0.171	0.257	1.81
8	7>M <u>></u> 6	10	0.782	$\log \epsilon_L$	log a	0.756	0.0554	0.222	1.67
8	6>M <u>></u> 5	26	0.680	$\log \epsilon_L$	log a	0.500	0.177	0.248	1.77
8	5>M	11	0.754	$\log \epsilon_L$	log a	0.403	0.349	0.204	1.60
9	_	46	0.716	$\log \epsilon_L^-$	log a	0,771	0.0147	0.305	2.02
10	_	26	0.791	$\log \epsilon_L$	log a	0.689	0.459	0.185	1.53
11	Δ≥150	21	0.862	$\log \epsilon_L$	log a	0.796	0.171	0.240	1.74
11	Δ<150	38	0.745	$\log \epsilon_L$	log a	0.570	0.137	0.253	1.79
12	_	59	0.830	$\log \epsilon_L$	$\log(\hat{a}_{x}\cdot T/2\pi)$	0.652	0.789	0.245	1.76
12	M≥7	12	0.944	$\log \epsilon_L$	$\log (a) \cdot T/2\pi$		0.804	0.134	1.36
12	7>M <u>></u> 6	10	0.847	log E _L	log (a • T/2π)		0.780	0.189	1.55
12	6>M>5	26	0.776	$\log \epsilon_L$	log (a • T/2π)		0.685	0.213	1.63
12	5>M	11	0.813	$\log \epsilon_L$	$\log (a_x \cdot T/2\pi)$		0.753	0.181	1.52
13		17	0.898	$\log \epsilon_L$	log v x	1.16	0.791	0.259	1.82

Table 5. Comparison of Observed Strains and Various Calculated Strains (Shimonaga Site)

М	ε _L (x10 ⁻⁶)	$a_{x}(gal)$	e_p/ϵ_L	e_{CL}/ε_{L}	e _{CG} /E _L	$e_{CT}^{/\varepsilon}_{L}$
7.4	299	125	1.0	1.7	2.2	3.0
M>7	13.9	7.2	1.3	2.1	2.7	3.7
7.3	12.2	8.3	1.7	2.8	3.6	4.9
6.3	24.8	14.8	1.5	2.4	3.1	4.3
5.8	6.1	5.9	2.4	4.0	5.1	7.0
5.8	19.4	48.6	6.1	10.2	13.2	17.9
5.8	16.5	52.8	7.8	13.0	16.8	22.8